

Broken Ladders: AI, Teamwork, and the Dynamics of Skill Formation in the Workplace*

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Abstract

We study the efficiency of AI adoption in knowledge work using a model of team production and learning. Seniors pick higher-value problems and solve the hardest tasks; juniors learn by working with them. AI can solve problems at a lower cost than juniors, but it lacks the ability to recognize the value of the problems it is solving. Its output has to be reviewed by a human; this supervision time is an important bottleneck for the productivity gains from adoption. AI raises output in the short run, but it can limit learning and decrease output in the long run. Inefficient AI adoption can be the result of seniors not internalizing the value of the mentoring they provide, or of AI or AI-using juniors crowding out (other) juniors from learning from seniors. Whether AI adoption is dynamically inefficient depends on the static gains from AI, and the magnitude of dynamic gains from learning.

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1 Introduction

Artificial intelligence (AI), especially generative AI, is reshaping how work is organized. Evidence from the U.S. Census Bureau suggests that 12-14% of large businesses already use AI tools in their operations (Census 2025). A growing concern is that these tools will displace entry-level jobs. Major technology companies—including Microsoft, Amazon, and Anthropic—have reportedly reduced hiring of interns and junior employees, choosing instead to rely on AI for tasks that junior staff used to perform. A similar mechanism might be driving the fact that employment in the youngest age group fell, while employment in other age groups did not (Brynjolfsson et al. (2025)). This pattern extends beyond the technology sector: senior lawyers now use AI to draft contracts, and expert developers leverage AI coding agents rather than delegating to junior colleagues.

In knowledge organizations, juniors learn from seniors through apprenticeship. A junior collaborating with a senior acquires expertise – technical skills and judgment about what problems matter – and eventually becomes a senior. If AI replaces juniors in production, it improves the productive efficiency of seniors in the short run. But AI also threatens to break the career ladder, halting the development of human skills and potentially lowering long-run output.

We develop a model to study this trade-off. Building on the framework of hierarchical team production (Garicano (2000), Garicano and Rossi-Hansberg (2006)), we add two key features. First, seniors and juniors differ not only in problem-solving skills but also in *value recognition*, the ability to identify which problems generate high revenue. Second, we incorporate *learning-by-mentoring*, juniors can learn both skills by working alongside seniors. We model AI as a tool with zero marginal cost that can solve problems up to some difficulty level, but lacks value recognition and requires human supervision. This supervision creates a binding resource constraint: AI adoption scales only up to what humans can oversee.

The Michelangelo thought experiment. To build intuition, consider a sculptor's workshop in Renaissance Florence. All sculptors can finish one sculpture per year if working alone. Senior sculptors, masters like Michelangelo, create beautiful, life-like sculptures. Junior sculptors can produce less refined, crude sculptures. Crucially, Michelangelo knows which commissions to accept. When the Medici request a tomb sculpture, he recognizes this as a high-value opportunity and commits, and earns 3 Ducats. When a minor guild offers the same nominal fee for a decorative fountain, he knows the project will drag on, specifications will change, and payment will never arrive. A junior sculptor would accept both indiscriminately, and occasionally spend months on a cancelled project, earning 1 Ducat per project on average. This ability to identify which problems are worth solving is *value recognition*. It is distinct from the technical skill of carving marble: a junior can learn to carve beautifully, but learning to read patrons, anticipate their tastes, and select profitable commissions takes years of experience working alongside a master.

Michelangelo can finish $n = 6$ sculptures per year if he does not have to carve the marble himself. With six junior sculptors working as apprentices, each carving one marble block, the workshop produces 18 Ducats of output. Junior wages are pinned by their outside option, which is to work solo in the suburbs and complete low-value projects, generating 1 Ducat. Michelangelo thus earns $6 \times 3 - 6 \times 1 = 12$ Ducats per year, which is four times his solo earnings, and more than ten times what a solo junior earns. Apprentices also learn: by year two, they become masters themselves. This is the career ladder.

Now Leonardo invents a marble-carving machine, rented at zero cost. In one scenario, Michelangelo fires all apprentices and instead uses 5 instances of the machine directly. With 5 machines he produces 15 Ducats of output, but now keeps it all, so earns more than by hiring junior apprentices. The juniors who would have been his apprentices still earn 1 Ducat each. The static gain from the machine is thus the 3 Ducats extra that Michelangelo earns. But no one is learning. In year two, there is still only one master

in Florence instead of seven. This generates the dynamic loss: in year two, instead of 7 masters earning 12 Ducats each, only 1 master earns 15 Ducats, while the other 6 would-be masters earn 1 Ducat each. Output in year 2 is 63 Ducats lower than would have been without the marble carving machine.

In another scenario, apprentices also have access to the machine if working with Michelangelo. Each apprentice can carve 1.5 marble blocks per year instead of one. Michelangelo can still only review 6 junior carved marbles, so he hires only 4 apprentices. The apprentices' wage is pinned down by solo juniors' earnings, who do not have access to the machine, and still earn 1 Ducat. Seniors now earn more, $6 \times 3 - 4 \times 1 = 14$, but all juniors, solo or apprentice earn the same. The static gain comes from the seniors earning more. However, only 4 people watch Michelangelo work, only 4 people learn, and only 4 people become masters. The career ladder has shrunk. In year 2 instead of 7 masters earning 12 Ducats each, 5 masters earn 14 Ducats each and 2 would-be masters earn 1 Ducat each. Output in year 2 is 12 Ducats lower than would have been without the marble carving machine.

Note what the marble-carving machine cannot do: it cannot judge which commissions Michelangelo should accept. The machine has no sense of which patrons are worth cultivating. Even with a perfect carving machine, Michelangelo must still review each block, decide which projects to pursue, and manage client relationships. This is why the senior's capacity constraint persists: AI does not free up Michelangelo's time for more projects, because the bottleneck was never the carving. The bottleneck is his judgment about what to carve.

Two sources of inefficiency. The thought experiment reveals two sources of inefficiency. First, when Michelangelo fires apprentices to use the machine directly, he does not internalize the value of the mentoring he provides. This is a pecuniary externality: if juniors could pay for training (via wage cuts), the externality would be internalized. With a wage cut of half a Ducat per apprentice, Michelangelo would not use the machine, and maintain the apprentice system. Second, when apprentices can use the machine themselves

and become more productive, fewer are needed in teams. Learning and work are bundled together in the apprenticeship model, you learn by being present while you work. The machine unbundles productivity from learning: a junior with the machine produces more, hence teams shrink, and fewer juniors learn. The higher productivity that comes with the machine crowds out juniors from learning.

Wage adjustments alone cannot restore the first-best. Knowledge is non-rival: training six apprentices is not one third less efficient than training four. With AI, optimal production calls for smaller teams, as each junior handles more problems, but optimal learning calls for larger teams, such that many juniors watch and learn from the senior. These objectives conflict. Part-time apprenticeships could help, with each junior working some time using AI for a senior and some time solo, but would require divisible jobs and a learning technology that does not depend on time spent working with a senior. If there is a minimum time threshold for effective learning, or production per junior does not scale linearly with time, the bundling cannot be undone.

Main results. We formalize these intuitions in a model where seniors have both higher problem-solving skills, $z_1 > z_0$, and better value recognition, $v_1 > v_0$. AI has skill z_A but no value recognition; all of its output must be reviewed by a human. AI does not resolve the senior's capacity constraint: the maximum number of junior problems a senior can handle is unchanged. Therefore, team output stays the same when juniors use AI, teams simply shrink.

Our model reveals that *without learning*, AI adoption is always efficient. Seniors' decisions to maintain or dissolve teams maximize GDP. *With external learning*, such that juniors learn but do not internalize the gains, seniors might make inefficient decisions whether to dissolve teams or reduce team size in response to the arrival of AI, which can result in lower long-run output. *With internalized learning*, such that juniors accept wage cuts that fully internalize the gains from learning, seniors' decisions are efficient. However, AI use can still be dynamically inefficient: while it raises short-run output, it can lower the long-run senior share enough that steady-state GDP falls.

Dynamic inefficiency is most likely when learning is fast, productivity gaps between seniors and juniors are large, and AI's static gains are modest. As AI improves, static gains grow and inefficiency becomes less likely. The value recognition gap persists even with perfect problem-solving AI, so human mentorship retains value.

Related literature. Our model extends the canonical model of hierarchical team production (Garicano (2000), Garicano and Rossi-Hansberg (2006)) to include AI and learning. In contemporaneous work, Ide and Talamàs (2025) explore the implication of AI in a similar framework, but their focus is on the relative gains of individuals with different skills, depending on whether AI is autonomous or not. Non-autonomous AI in their framework can only give advice on hard problems, i.e., act as a senior in our framework. Autonomous AI on the other hand can take the role of both juniors and seniors. We have a fundamentally different view. We assume that AI can solve problems up to a certain difficulty, but it gives an answer to any question it is asked. Since it cannot clearly communicate whether it has solved a problem or not, humans need to check whether AI's solution is correct, hence AI requires human supervision. Therefore, in our setup AI can only take the place of a junior worker, including the possibility that it becomes the junior of a junior. We view AI as non-autonomous, because it needs human supervision, it cannot be trusted with leading teams. On the other hand, AI can be tasked with solving problems, as juniors can be, but its output must be checked. This distinction matters because our setup creates a bottleneck that AI cannot resolve, leading to the crowding out of juniors that is central to our analysis.

We view our main contribution to lie in explicitly modeling learning in teams, and in assessing how the reliance on AI for production alters learning dynamics and the gains from AI. This connects to the literature on learning on the job (Arrow (1962), Becker (1962), Ben-Porath (1967), Lucas (1988)). In those models, as long as somebody works, they learn and accumulate human capital. A more recent literature explores how learning at the workplace impacts aggregate growth (Burstein and Monge-Naranjo (2009), Jovanovic (2014). Caicedo et al. (2019) incorporate learning in the canonical model of Gari-

cano (2000), but learning happens not in teams but via random meetings with others. In two recent papers, Jarosch et al. (2021) and Herkenhoff et al. (2024) empirically measure the extent to which a worker's on-the-job human capital accumulation is impacted by their co-workers. Both papers find that only those co-workers matter for learning who are more skilled than the worker. Herkenhoff et al. (2024) point out that some types of technological changes by changing the sorting of workers into teams can lead to lower long-run output, which echoes our findings. To the best of our knowledge, ours is the first paper that extends the canonical model of Garicano (2000) with explicitly modeling learning in teams from seniors. This extension shows that working in teams generates additional benefits by shifting the steady state distribution of skills in the economy. Including AI in such a framework highlights a potential dynamic externality in AI adoption due to lost learning opportunities because of AI's impact on teams. Beraja and Buera (2026) show that dynamic competition can lead private incentives to deviate from social optima, though not always—some equilibria are constrained-efficient. Our welfare results have a similar flavor: private incentives can deviate from social optima for seniors if learning is not priced, and because the higher productivity of juniors with AI crowds out other juniors from learning.

In a similar vein, Acemoglu and Restrepo (2018) and (2020) emphasize that automation must be sufficiently productive and counterbalanced by new tasks, otherwise displacement costs outweigh gains for workers. In their framework, output always increases with automation, the problem is purely distributional. Our results emphasize a dynamic inefficiency: due to the threat of breaking the learning ladder, AI use can reduce output in the long run, while in the short run everyone uses it efficiently. AI can disrupt knowledge transfer in other domains too: Koren et al. (2026b) show that AI-assisted coding reduces the feedback loops that sustain open-source software communities.

Recent empirical work explores AI's impact on training. Hess et al. (2023) find reduced training in high-automation-risk jobs. Muehlemann (2025) documents that German firms adopting AI cut training for current workers but increased apprenticeships. Brynjolfsson

et al. (2025) show that generative AI can accelerate learning: novice customer support workers improved with AI assistance. Noy and Zhang (2023) find similar effects for writing. These studies suggest AI could serve as a training device rather than a substitute for mentorship—a mechanism we abstract from but that could mitigate the dynamic losses we identify if AI-based learning proves to be a close substitute for mentoring.

The remainder of the paper proceeds as follows. Section 2 presents the model, we then analyze equilibrium without learning in Section 3 and with learning in Section 4, and we discuss sources of inefficiency in Section 5. Section 6 concludes.

2 Model setup

This section presents the model, describing the environment.

Problems and worker types. Problems have varying difficulties and values. Formally, let task difficulty Z be uniformly distributed on $[0, 1]$. A worker’s skill level $z \in (0, 1)$ represents the hardest problem that they can solve: a person with skill z_i can solve all problems with difficulty $Z \leq z_i$ with certainty, but cannot solve any problem with $Z > z_i$.

We assume that there are two types of workers, who differ in their skill levels: juniors with skill z_0 and seniors with skill z_1 , where $z_1 > z_0$. Seniors and juniors also differ in their ability to recognize problem value, v_i . The value of a problem is the revenue it generates if solved. Seniors draw problems with higher expected values than juniors, that is $v_1 > v_0$. This could be micro-founded by individuals drawing problems from some value distribution and deciding whether to attempt to solve them or to discard them: if seniors are better at judging value, they end up with higher expected value of attempted problems.

Demographics and learning. Time is continuous. At any given point in time, δL people are born (we normalize $L = 1$). A fraction ϕ of individuals are born with senior skills and value recognition (z_1, v_1) , and fraction $1 - \phi$ with junior attributes (z_0, v_0) . All individuals

die with a Poisson arrival rate of δ , independent of skill.

The model allows for stochastic learning by juniors, in which case their skill level changes to z_1 and their value recognition to v_1 . We consider two learning scenarios, no learning and learning-by-mentoring. In the no learning scenario, the skill distribution is static. In the learning-by-mentoring scenario, juniors working in teams learn from seniors at rate λ .

Working solo. Working on a problem requires time, committed before knowing the difficulty. One problem takes one unit of time to work on. If a person is working alone, called solo work, they can solve it with probability z_i , so their expected output per unit of time is $y_i \equiv v_i z_i$. These values also pin down their solo wage in a competitive market: working alone, a junior earns $w_{0,solo} = y_0$ per unit of time, and a senior earns $w_{1,solo} = y_1$.

Working in teams. Now consider teamwork: a senior can collaborate with several juniors. Seniors draw problems for everyone on their team, at expected value v_1 , and juniors attempt to solve all the problems first. Juniors solve the easier problems that they are capable of, and escalate the unsolved harder problems, those with $Z > z_0$ to the senior. The senior then spends time handling those tougher problems.

We assume that whenever a junior brings a problem to the senior, the senior spends $h < 1$ units of time on it, whether or not the senior eventually manages to solve it. The parameter h captures the time cost per problem of communication, mentoring, and problem-solving. The condition $h < 1$ means it is more efficient for a senior to solve a problem brought by a junior than to solve it alone. Intuitively, the junior filters and only forwards the harder subset of problems to the senior. The senior's time constraint requires that, in expectation, they must be able to handle all the problems that juniors send to them.

Working with AI. AI systems work like subordinates in a team: humans give problems to the AI, the AI attempts to solve all problems, and passes on the output to the human. The AI provides a solution to all problems, but it can solve problems only up to diffi-

culty z_A . Because the AI pretends to solve all problems, each attempted problem by the AI requires human time. For problems with $Z \leq \min\{z_A, z_i\}$, the review takes $h_{A1} < 1$ time. This captures the insight that when the AI provides a correct solution *and* the difficulty of the problem does not exceed the human's skill level, the review process is fast. This review time is important, because it captures the resource constraint that AI creates through the need for human verification. For problems with $Z > \min\{z_A, z_i\}$, reviewing and solving takes $h_{A2} \in (h_{A1}, 1]$ time. When the AI cannot provide a correct solution *or* the difficulty of the problem is above the human's skill level, reviewing and/or solving the problem takes long. This implies that workers can effectively use AI capabilities up to their own skill level. This review constraint is crucial: it implies that AI does not relax the senior's capacity constraint, and thus does not increase team output, it only shrinks teams.

3 Equilibrium in the no learning economy

In our baseline model there is no learning: each individual keeps the skill they were born with. This is a static model, where the measure of juniors is $L_0^{NL} = 1 - \phi$ and the measure of seniors is $L_1^{NL} = \phi$ at all times. We first analyze this economy without AI, then introduce AI and study how it affects outcomes.

3.1 Equilibrium without AI

Solo output and wages. As discussed before, when working solo, expected output equals the probability of solving a random problem times its expected value:

$$Q_{i,solo}^{NL} = w_{i,solo}^{NL} = v_i z_i = y_i. \quad (1)$$

This says that a solo junior produces $y_0 = v_0 z_0$ and a solo senior produces $y_1 = v_1 z_1$ per unit of time.

Team size and output. The senior's time constraint pins down the maximum team size. Since juniors pass on problems with difficulty $Z > z_0$, which occurs with probability $1 - z_0$, and each escalated problem takes h of the senior's time, a senior with n_0 juniors spends $n_0(1 - z_0)h$ time on escalated problems. Setting this equal to the senior's total time yields:

$$n_0 = \frac{1}{h(1 - z_0)}. \quad (2)$$

This is the *maximum number of junior problems* that a senior can handle. Team output is the sum of the value of problems that juniors solve and those that the senior solves:

$$Q_{team}^{NL} = n_0 v_1 z_0 + n_0 v_1 (1 - z_0) \frac{z_1 - z_0}{1 - z_0} = n_0 v_1 z_1 = \frac{y_1}{h(1 - z_0)}. \quad (3)$$

The senior essentially multiplies their expertise across n_0 problems by hiring n_0 juniors. Seniors can be highly productive when supported by a team: if communication is more efficient, h is smaller, and juniors pass on only the harder problems, z_0 is larger, a senior can leverage a larger team.

Participation constraint. Teamwork is better than solo work if team output exceeds the sum of individual outputs, $n_0 y_0 + y_1$:

$$\frac{y_1}{y_0} > \frac{n_0}{n_0 - 1} = \frac{1}{1 - h(1 - z_0)}. \quad (\text{PC})$$

This requires the senior's productivity to be sufficiently large relative to the junior's productivity. The threshold depends on the efficiency of teamwork: if h is smaller or z_0 is larger, teamwork is more efficient, and the productivity gap between seniors and juniors need not be as large. We assume that this *participation constraint* holds throughout.

Labor market equilibrium. If teamwork is better than solo work, as many teams form as possible. We assume that *juniors are abundant*, meaning that all seniors can lead teams of n_0 juniors, and there are some juniors who cannot join teams. This case arises if $L_0 > n_0 L_1$,

which requires $\phi < h(1 - z_0)/[1 + h(1 - z_0)]$. We assume throughout that this condition holds. The excess juniors work solo and earn $w_{0,solo}^{NL} = y_0$. Competition among juniors implies that juniors in teams also earn y_0 ; if offered less, they would work solo; if offered more, juniors outside of teams would undercut them. In this case, seniors extract all the surplus and their wage is given by

$$w_{1,team}^{NL} = Q_{team}^{NL} - n_0 w_{0,solo}^{NL} = n_0(y_1 - y_0) = \frac{y_1 - y_0}{h(1 - z_0)}. \quad (4)$$

Seniors prefer teams over solo work if $w_{1,team}^{NL} > w_{1,solo}^{NL}$, which holds exactly when the participation constraint (PC) is satisfied.

Aggregate output and efficiency. Aggregate output is the sum of team output and solo output of juniors who could not join teams:

$$Y_{teams}^{NL} = L_1^{NL} n_0 y_1 + (L_0^{NL} - n_0 L_1^{NL}) y_0 = \phi n_0 (y_1 - y_0) + (1 - \phi) y_0, \quad (5)$$

which is equal to total wages paid to seniors and to juniors. If everyone worked solo, output would be $Y_{solo}^{NL} = \phi y_1 + (1 - \phi) y_0$. Comparing these immediately yields that aggregate output with teams is higher than aggregate output from solo work if and only if (PC) holds. This means that *team formation is efficient*: the participation constraint that makes seniors willing to form teams is exactly the condition under which team formation raises GDP.

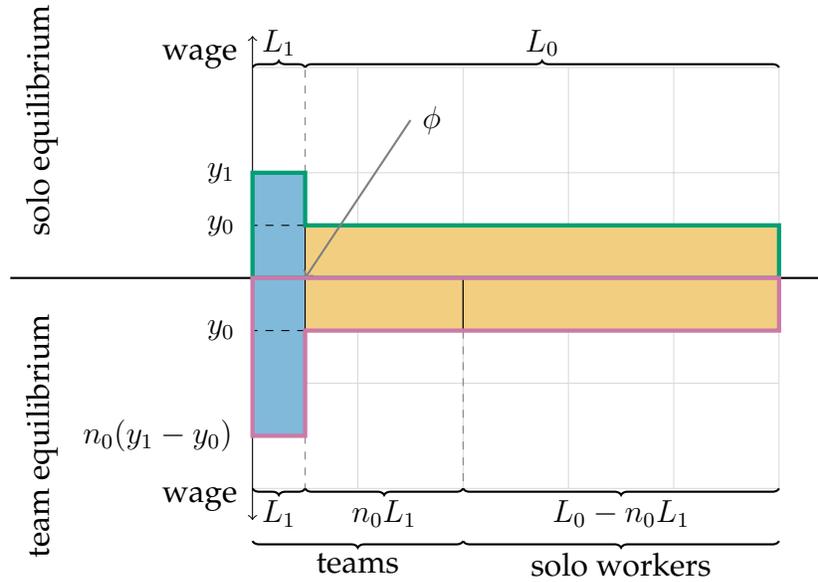


Figure 1: Output and wages in the baseline economy

Notes: The horizontal axis shows the share of seniors and juniors in the economy. The vertical axis shows wages when working solo above the horizontal axis, and when working in teams below the horizontal axis.

Figure 1 illustrates the equilibrium. The horizontal axis represents the share of seniors, ϕ , and the share of juniors, $1 - \phi$. The top part, above the horizontal axis, shows on the vertical axis income for all workers when everyone works solo: seniors earn y_1 , shown in blue, and juniors earn y_0 , shown in yellow. Aggregate output, Y_{solo}^{NL} , is the sum of all earnings and is shown with the green outline. The bottom part shows on the vertical axis income for all workers in case of team formation. Each senior hires n_0 juniors, and seniors earn $n_0(y_1 - y_0)$ (in blue), while juniors in teams as well as when solo earn y_0 (in yellow). Aggregate output, Y_{teams}^{NL} , is the sum of total earnings and is shown with the red outline. When the participation constraint holds and only then does team output exceeds solo output: juniors earn the same whether teams are formed or not, and if and only if (PC) holds does the senior wage in teams exceed senior solo wage.

3.2 Equilibrium with AI

Now suppose AI is available to all workers, with capability $z_A \leq z_0$. Recall that for problems with difficulty $Z \leq \min\{z_A, z_i\}$ it takes h_{A1} time to review AI's output. For problems exceeding this difficulty, the time required is h_{A2} , and only problems up to difficulty z_i are solved. Therefore, given the capacity of each worker, if $z_A \leq z_0$, each can handle

$$n_A = \frac{1}{h_{A1}z_A + h_{A2}(1 - z_A)} \quad (6)$$

AI instances. Solo output and wages with AI are therefore

$$Q_{i,solo}^{NL,AI} = w_{i,solo}^{NL,AI} = n_A z_A v_i + n_A (1 - z_A) \frac{z_i - z_A}{1 - z_A} v_i = n_A y_i. \quad (7)$$

AI amplifies skills: when $n_A > 1$, both juniors and seniors produce and earn more when using AI than without.¹

Note that if $z_A \in (z_0, z_1]$, then seniors can handle n_A instances as defined above, whereas juniors can handle $\bar{n}_{A0} \equiv 1/[h_{A1}z_0 + h_{A2}(1 - z_0)]$. If $z_A > z_1$, then seniors can handle $\bar{n}_{A1} \equiv 1/[h_{A1}z_1 + h_{A2}(1 - z_1)]$ instances of AI, while juniors can handle \bar{n}_{A0} instances. In what follows, we will denote the number of AI instances worker type i can handle with $n_{Ai} \equiv \min\{n_A, \bar{n}_{Ai}\}$, to make it clear which worker's AI productivity gain is relevant. The expression of solo output and wage remains as in (7) even if $z_0 < z_A$, except n_{Ai} is required instead of n_A .²

Impact on team work. When juniors can use AI in teams, each junior can handle at most n_{A0} problems with AI, passing on problems with $Z > z_0$ to the senior. The senior's capacity constraint still binds: the senior can handle at most n_0 escalated problems that

¹Note that our model differs in this aspect from the setup in the Michelangelo thought experiment, there only those juniors could use the carving machine who worked as an apprentice with Michelangelo.

²All following expressions need to be expressed separately depending on whether z_A is below or above z_0 and z_1 . The formulas end up being the same in all cases, in the text we derive expressions assuming $z_A \leq z_0$.

have been previously handled by juniors. To minimize wage costs, the senior asks juniors to use as many AI instances as they can handle. Since each junior now escalates $n_{A0}(1 - z_0)$ problems, the capacity constraint of the senior implies a lower team size than without AI:

$$n_0^{AI} = \frac{n_0}{n_{A0}}. \quad (8)$$

Team output remains unchanged:

$$Q_{team}^{NL,AI} = n_0^{AI} n_{A0} z_A v_1 + n_0^{AI} n_{A0} (1 - z_A) \frac{z_0 - z_A}{1 - z_A} v_1 + n_0^{AI} n_{A0} (1 - z_0) \frac{z_1 - z_0}{1 - z_0} v_1 = n_0 y_1. \quad (9)$$

This is the key insight: AI makes each junior more productive, but the senior's bottleneck, the maximum number of junior problems they can handle, is unchanged. AI therefore shrinks teams without raising team output. AI simply allows each junior to process more problems before escalating, which means fewer juniors are needed for the same team output. But since each junior's wage is now higher due to AI increasing their productivity, seniors' team wage also remains unchanged:

$$w_{1,team}^{NL,AI} = Q_{team}^{NL,AI} - n_0^{AI} w_{0,solo}^{NL,AI} = n_0 (y_1 - y_0).$$

Seniors' decision to maintain or dissolve teams. Seniors compare their team wage to their solo wage with AI. They choose to dissolve teams if

$$n_{A1} y_1 > n_0 (y_1 - y_0). \quad (\text{DISS})$$

When this condition holds, seniors prefer to work alone using AI rather than lead teams of juniors who use AI.

Efficiency of seniors' decision. If seniors maintain teams, aggregate output is:

$$Y_{teams}^{NL,AI} = \phi n_0 (y_1 - y_0) + (1 - \phi) n_{A0} y_0.$$

If seniors dissolve teams, aggregate output is:

$$Y_{solo}^{NL,AI} = \phi n_{A1}y_1 + (1 - \phi)n_{A0}y_0.$$

Aggregate output when everyone works solo exceeds aggregate output from teamwork if and only if seniors' solo wage is higher than their wage in teams. This implies that seniors' decision is efficient: they maintain teams exactly when doing so maximizes GDP.

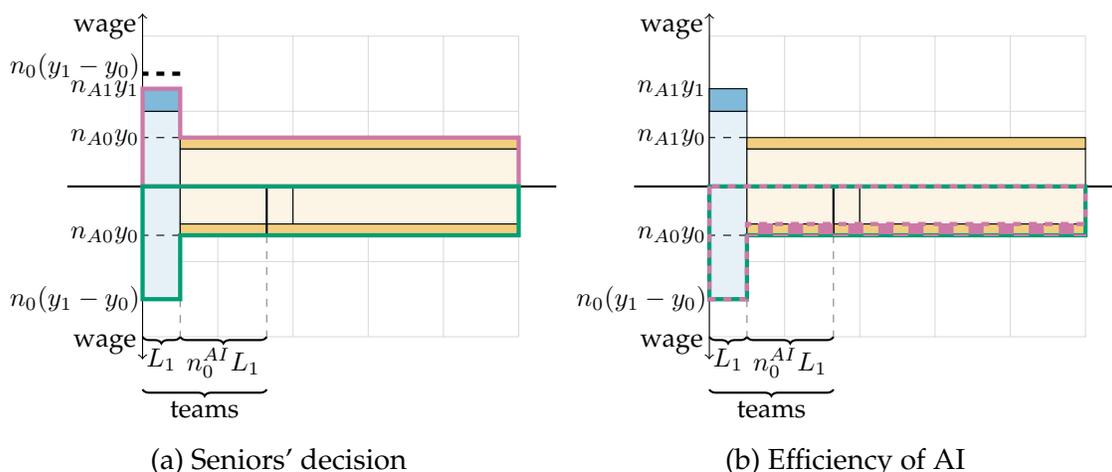


Figure 2: Impact of AI on output.

Notes: The horizontal axis shows the share of seniors and juniors in the economy. The vertical axis shows wages when working solo above the horizontal axis, and when working in teams below the horizontal axis. The left figure compares aggregate solo output with AI to aggregate team output with AI. The right figure compares aggregate team output without AI to aggregate output with AI.

The efficiency of seniors' decision is illustrated in Figure 2a. The darker blue and yellow regions show that solo output increases for seniors to $n_{A1}y_1$ and for juniors to $n_{A0}y_0$. Below the horizontal axis we can see that the wages of solo and team juniors increase to $n_{A0}y_0$. Senior team wages remain unchanged in the economy with AI use, but the size of teams shrinks to n_0^{AI} , implying fewer workers in teams. Seniors decide to maintain teams if and only if $n_0(y_1 - y_0) > n_{A1}y_1$, and in this case aggregate output is also higher with teams (shown in green outline) than without (shown with red outline), therefore seniors' decision is efficient.

Efficiency of AI adoption. To evaluate whether AI use is efficient, we need to compare aggregate output without AI to output with AI, whether teams are maintained or dissolved. The income of solo and team juniors is strictly higher with AI than without, as $n_{A0}y_0 > y_0$. Senior wage is weakly higher with AI. If teams are maintained, then senior wages are the same as before, whereas if teams are dissolved, then senior wages are strictly higher with AI, as that is the condition for dissolving teams. Therefore, AI adoption is always efficient in the no-learning economy. This is shown in Figure 2b, for a case where with AI teams are maintained. If teams are maintained, senior wage, and total senior income is the same as without AI. But all juniors' productivity and earnings are higher with AI than without, which leads to a gain in aggregate output, indicated by the red checkered area.

Result 1: Without learning, seniors make efficient decisions about whether to maintain or dissolve teams, and AI adoption is always efficient.

AI capability improvements. The impact of improvements in AI capability depends on the level of z_A relative to human skills. As long as $z_A \leq z_0$, junior and senior solo productivity with AI increases as z_A increases, and the size of teams shrinks further. At $z_A = z_0$, junior AI use is maximized at $\bar{n}_{A0} = 1/[h_{A1}z_0 + h_{A2}(1 - z_0)]$, and no further improvement in junior productivity can be obtained. For AI improvements in the $z_0 < z_A \leq z_1$ range, senior solo productivity with AI keeps on improving, and is maximized at $\bar{n}_{A1} = 1/[h_{A1}z_1 + h_{A2}(1 - z_1)]$. Beyond this point, AI improvements do not generate any productivity gains, as verification becomes the bottleneck. If $\bar{n}_{A1}y_1 > n_0(y_1 - y_0)$, then there exists a threshold AI capability z_A^* at which seniors optimally decide to dissolve teams.

4 Equilibrium in the economy with learning

We now add learning by assuming that juniors can become seniors over time if they work in teams. This is the mechanism that AI threatens: if teams shrink or dissolve, fewer ju-

niors learn, and the long-run supply of seniors falls. Learning captures career progression through on-the-job training: a junior who collaborates with a senior gradually acquires senior-level skills and value recognition. We model this as a Poisson process: while working in a team, a junior becomes a senior at rate λ .

4.1 Steady state without AI

The stock of seniors evolves according to:

$$\dot{L}_1 = \phi\delta - \delta L_1 + \lambda L_1 n_0,$$

where $\phi\delta$ is the inflow of individuals born as seniors, δL_1 is the outflow due to death, and $\lambda L_1 n_0$ is the inflow due to learning. We assume that juniors remain abundant even in the economy with learning, that is $L_0 > n_0 L_1$ at all times, implying that each senior has a full team of seniors, and $L_1 n_0$ juniors work in teams. The steady state share of seniors is given by

$$L_1^* = \frac{\phi}{1 - \frac{\lambda}{\delta} \frac{1}{h(1-z_0)}} = \frac{\phi}{1 - \frac{\lambda}{\delta} n_0}. \quad (10)$$

This is well-defined and juniors remain abundant if $\lambda/\delta < (1 - \phi)h(1 - z_0) - \phi$. Learning by mentoring raises the long-run proportion of seniors: $L_1^* > \phi$. The faster the learning rate λ or the larger is team size n_0 , the greater the boost to human capital.

Aggregate output with learning. Steady state output with learning is the sum of total team output and total solo junior output:³

$$Y_{teams}^{*LE} = L_1^* n_0 y_1 + (1 - L_1^* - L_1^* n_0) y_0 = L_1^* n_0 (y_1 - y_0) + (1 - L_1^*) y_0. \quad (11)$$

³Calculated as the number of seniors times team output, plus the number of solo juniors times solo junior output.

It can be verified that this is equal to the sum of earnings in the no-learning economy, $w_{1,team}^{NL}$ for seniors, and $w_{0,solo}^{NL}$ for all juniors, but with a higher senior share. Note that when there is learning, junior wages in teams are not necessarily equal to solo junior wages. If juniors anticipate that by working in teams they might become seniors, they can internalize these gains and accept a wage cut as team juniors in exchange for learning. Whether learning gains are internalized or not does not change aggregate output, it just changes how team output is split between the senior and junior members of the team.

Wages when learning is fully internalized. Suppose juniors anticipate career progression and accept lower wages in teams in exchange for learning opportunities. In a competitive labor market with forward-looking workers and abundant juniors, a junior's expected lifetime utility from working in a team should equal that from working solo.

Let $J_{0,team}$ denote the expected present value of being a junior in a team:

$$\delta J_{0,team} = w_{0,team} + \lambda [J_{1,team} - J_{0,team}],$$

where $J_{1,team} = w_{1,team}/\delta$ is the present value of earnings as a senior. Solving yields

$$J_{0,team} = \frac{w_{0,team} + \frac{\lambda}{\delta} w_{1,team}}{\delta + \lambda}.$$

The value of being a solo junior is $J_{0,solo} = y_0/\delta$. Indifference of juniors between solo and team work requires $J_{0,team} = J_{0,solo}$, leading to

$$w_{0,team} = y_0 - \frac{\lambda}{\delta} (w_{1,team} - y_0). \quad (12)$$

This shows that juniors in teams accept a wage *below* their solo marginal product y_0 , because they expect to recoup the difference when they become seniors. We can write this wage cut as $\Delta = \frac{\lambda}{\delta} (w_{1,team} - y_0)$, so $w_{0,team} = y_0 - \Delta$. Juniors effectively pay for training via a wage discount.

The senior's wage is team output minus wages paid to juniors:

$$w_{1,team} = n_0(y_1 - w_{0,team}),$$

from which, after substituting the expression for $w_{0,team}$ and solving, we get that senior wage in teams is

$$w_{1,team}^{IL} = \frac{n_0 \left(y_1 - y_0 \left(1 + \frac{\lambda}{\delta} \right) \right)}{1 - \frac{\lambda}{\delta} n_0}. \quad (13)$$

This exceeds the senior wage without internalized learning, $n_0(y_1 - y_0)$, because juniors accept wage cuts. The senior wage is increasing in the learning speed λ/δ , as faster learning means juniors accept larger wage cuts. Junior wage in teams is given by

$$w_{0,team}^{IL} = y_0 - \frac{\lambda n_0 (y_1 - y_0) - y_0}{1 - \frac{\lambda}{\delta} n_0}.$$

Juniors' wage cannot be negative, thus the wage cut cannot be larger than y_0 . When the non-negativity constraint on junior team wages binds, then junior team wages cannot fully internalize learning gains. The condition under which wages can fully internalize the gains from learning is

$$\frac{\lambda}{\delta} < \frac{y_0}{n_0 y_1 - y_0}.$$

If the speed of learning is too high, or junior productivity is too low relative to senior productivity and the gains from teams, then this condition does not hold, and juniors will work for free in teams, and wages do not fully internalize the gains from learning.

Efficiency of team formation with learning. Steady state aggregate output if teams are formed, Y_{teams}^{*LE} , exceeds steady state solo output, Y_{solo} , if

$$\frac{\phi}{1 - \frac{\lambda}{\delta}n_0}n_0(y_1 - y_0) + \left(1 - \frac{\phi}{1 - \frac{\lambda}{\delta}n_0}\right)y_0 > \phi y_1 + (1 - \phi)y_0,$$

which can be shown to be equivalent to $w_{1,team}^{LL} > w_{1,solo}$. This implies that as long as wages fully internalize the dynamic gains from learning, seniors' decision to form teams is dynamically efficient: they form teams precisely when team formation raises long-run GDP. However, if wages do not fully internalize learning gains, for example because learning gains are too large relative to junior solo productivity, then teams might not be formed, even though steady state aggregate output would be higher if teams were formed. Thus the non-formation of teams can be dynamically inefficient.

Result 2: With internalized learning, the wage mechanism internalizes the value of mentoring and team formation is efficient.

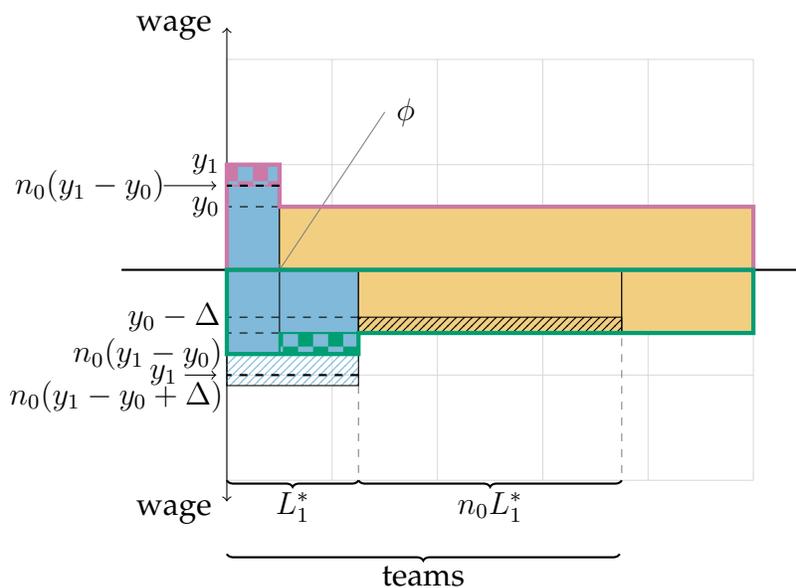


Figure 3: Learning-by-mentoring and internalized learning.

Notes: The horizontal axis shows the share of seniors and juniors in the economy. The vertical axis shows wages when working solo above the horizontal axis, and when working in teams below the horizontal axis.

Figure 3 shows the steady state of the economy if everyone works solo above the horizontal axis, and the steady state of the economy if teams are formed below the horizontal axis. In the solo economy, the senior wage is y_1 , and junior wage is y_0 . The red outline shows steady state aggregate solo output, Y_{solo} . If there is learning, then working in teams expands the senior stock to $L_1^* > \phi$. If wages do not internalize learning gains, then senior team wage is $n_0(y_1 - y_0)$, and junior team and solo wage is y_0 . The green outline shows steady state aggregate output if working in teams, Y_{teams}^{*LE} . With internalized learning, juniors accept a wage cut Δ (yellow hatched area) in exchange for career progression, while seniors receive a wage premium (blue hatched area). The senior team wage rises to $n_0(y_1 - y_0 + \Delta)$. In this configuration, steady state output is higher if teams are formed, which can be seen by comparing the red checkered area (the gain from higher senior solo wages) to the green checkered area (the gain from having more seniors each leading teams). If learning gains are not sufficiently internalized in wages, then since $y_1 > n_0(y_1 - y_0)$ seniors choose not to form teams. However, if wages fully internalize learning gains, senior wages are $n_0(y_1 - y_0 + \Delta) > y_1$, and therefore seniors prefer to lead teams of juniors rather than working solo. The wage cut Δ exactly internalizes the dynamic gains from team formation, making team formation efficient.

4.2 Equilibrium with AI and learning

Now suppose AI, with $z_A \leq z_0$, arrives in an economy at its learning steady state with teams. Solo juniors always use AI, as $n_{A0} > 1$, raising juniors' outside option to $n_{A0}y_0$. Two things can happen, either seniors maintain teams, but teams shrink and seniors hire $n_0^{AI} = n_0/n_{A0}$ juniors, or seniors decide to dismiss teams and use AI solo. In either case the inflow of seniors decreases, either learning slows down because fewer juniors work in teams, or learning ceases altogether. In what follows we analyze whether seniors make the efficient decision, and whether AI use in general is dynamically efficient.

Outcomes if teams are maintained. If teams are maintained, the steady state share of seniors is:

$$L_1^{*AI} = \frac{\phi}{1 - \frac{\lambda}{\delta} \frac{n_0}{n_{A0}}} < L_1^*. \quad (14)$$

The senior share is lower with AI because each team has fewer juniors learning.

Steady state output in teams is the sum of total team output and total solo junior output:⁴

$$Y_{teams}^{*LE,AI} = L_1^{*AI} n_0 y_1 + (1 - L_1^{*AI} - L_1^{*AI} \frac{n_0}{n_{A0}}) n_{A0} y_0 = L_1^{*AI} n_0 (y_1 - y_0) + (1 - L_1^{*AI}) n_{A0} y_0. \quad (15)$$

Which again can be expressed as the sum of earnings in the no-learning economy, $w_{1,team}^{NL}$ for seniors, and $w_{0,solo}^{AI}$ for juniors, but with the relevant steady state senior share. Note that again, team output can be split in different ways between seniors and team juniors. If workers do not internalize the gains from learning, then team juniors earn $n_{A0} y_0$, and seniors keep the rest of team output, $n_0 (y_1 - y_0)$. If workers internalize the gains, then team junior wages will be lower, and senior wages will be higher.

When learning gains are fully internalized in wages, following the same steps as before, we can show that junior team wage with AI satisfies:

$$w_{0,team} = n_{A0} y_0 - \frac{\lambda}{\delta} (w_{1,team} - n_{A0} y_0),$$

while senior team wage is given by $w_{1,team} = n_0 y_1 - n_0^{AI} w_{0,team}$, and solving for the senior wage we get that:

$$w_{1,team}^{IL,AI} = \frac{n_0 (y_1 - y_0 (1 + \frac{\lambda}{\delta}))}{1 - \frac{\lambda}{\delta} \frac{n_0}{n_{A0}}}. \quad (16)$$

⁴Calculated as the number of seniors times team output plus the number of solo juniors times solo junior output.

The senior's team wage is higher when learning is internalized, making dissolution less attractive. Senior wage is increasing in the learning speed λ/δ , in the number of junior problems the senior can handle, n_0 , and is decreasing in the productivity enhancement of AI, n_{A0} . The junior team wage that fully internalizes learning gains is given by

$$w_{0,team}^{IL,AI} = n_{A0}y_0 - \frac{\lambda n_0(y_1 - y_0) - n_{A0}y_0}{1 - \frac{\lambda n_0}{\delta n_{A0}}}.$$

For junior wages to fully internalize learning gains, the wage cut cannot exceed junior solo wages, $n_{A0}y_0$, as juniors cannot earn negative wages. Wages can fully internalize the gains from learning if

$$\frac{\lambda}{\delta} < \frac{n_{A0}y_0}{n_0y_1 - n_{A0}y_0}. \quad (17)$$

Seniors dissolve teams if $n_{A1}y_1 > w_{1,team}^{IL,AI}$, which if (17) holds boils down to the following:

$$\frac{\lambda}{\delta} < \frac{n_{A1}y_1 - n_0(y_1 - y_0)}{n_0 \left(\frac{n_{A1}}{n_{A0}}y_1 - y_0 \right)}. \quad (18)$$

If (17) does not hold, then juniors in teams receive no wages, and seniors dissolve teams if $n_0y_1 < n_{A1}y_1$.

Efficiency of seniors' decision. To determine whether seniors' decision is efficient we need to compare $Y_{teams}^{*LE,AI}$ with $Y_{solo}^{AI} = \phi n_{A1}y_1 + (1 - \phi)n_{A0}y_0$. Steady state aggregate team output exceeds solo output if

$$\frac{\phi}{1 - \frac{\lambda n_0}{\delta n_{A0}}} n_0(y_1 - y_0) + \left(1 - \frac{\phi}{1 - \frac{\lambda n_0}{\delta n_{A0}}} \right) n_{A0}y_0 > \phi n_{A1}y_1 + (1 - \phi)n_{A0}y_0,$$

which can be shown to be equivalent to $w_{1,team}^{IL,AI} > w_{1,solo}^{AI}$ if (17) is satisfied. Therefore, if wages fully internalize the gains from learning, senior's decision to form teams is dynamically efficient. On the other hand, if wages do not fully internalize the gains from

learning and $n_0 < n_{A1}$, then seniors dissolve teams, and if also $Y_{teams}^{*LE,AI} > Y_{solo}^{AI}$, then seniors' decision to dissolve teams leads to dynamic inefficiency.

Result 3: With internalized learning, seniors' AI adoption decisions are efficient. If learning gains are not fully internalized, seniors may over-adopt AI and dissolve teams, even if it lowers output in the long-run.

Efficiency of AI adoption. Even if seniors' decision is efficient, given AI availability, AI use itself may be dynamically inefficient. To determine whether this is the case, we need to compare long-run output with AI to long-run output without AI.

When teams are maintained with AI. AI use is dynamically inefficient if $Y_{teams}^{*LE,AI} < Y_{teams}^{*LE}$:

$$\frac{\phi}{1 - \frac{\lambda}{\delta} \frac{n_0}{n_{A0}}} n_0 (y_1 - y_0) + \left(1 - \frac{\phi}{1 - \frac{\lambda}{\delta} \frac{n_0}{n_{A0}}}\right) n_{A0} y_0 < \frac{\phi}{1 - \frac{\lambda}{\delta} n_0} n_0 (y_1 - y_0) + \left(1 - \frac{\phi}{1 - \frac{\lambda}{\delta} n_0}\right) y_0,$$

which holds if

$$\frac{(1 - \phi) n_{A0}}{n_0^2 \left(\phi \frac{y_1 - y_0}{y_0} + 1\right) + (1 - \phi)(n_{A0} + 1)} < \frac{\lambda}{\delta}.$$

The gain of AI comes from higher solo junior productivity, $n_{A0} y_0 > y_0$, while the loss comes from there being fewer seniors, $L_1^{*AI} < L_1^*$. AI use is dynamically inefficient if the loss dominates the gains. Dynamic inefficiency of AI is increasing in the learning speed, λ/δ , the productivity gap, y_1/y_0 , seniors' capacity to handle junior problems, n_0 , share of born seniors, ϕ , and is decreasing in AI's productivity multiplier for juniors, n_{A0} .

When teams dissolve with AI. AI use is dynamically inefficient if $Y_{solo}^{AI} < Y_{teams}^{*LE}$:

$$\phi n_{A1} y_1 + (1 - \phi) n_{A0} y_0 < \frac{\phi}{1 - \frac{\lambda}{\delta} n_0} n_0 (y_1 - y_0) + \left(1 - \frac{\phi}{1 - \frac{\lambda}{\delta} n_0}\right) y_0,$$

which is equivalent to

$$\frac{1}{n_0} \left[1 - \phi \frac{n_0 \frac{y_1}{y_0} - (n_0 + 1)}{\phi n_{A1} \frac{y_1}{y_0} + (1 - \phi)n_{A0} - 1} \right] < \frac{\lambda}{\delta}.$$

Again, dynamic inefficiency is more likely to arise if the learning speed is high, teams without AI and productivity gaps are large, and is less likely if AI is more capable.

Result 4: AI can be dynamically inefficient even when adoption decisions are privately optimal. This occurs when learning is fast, productivity gaps and teams without AI are large, and AI's static gains are modest.

4.3 AI capability improvements

To study the impact of AI capability improvements in dynamic inefficiency, it is informative to summarize the conditions under which dynamic inefficiency can arise. Table 1 summarizes the cases that can arise in the economy with internalized learning and AI and the conditions for dynamic inefficiency. It is clear from this table that the key to dy-

Table 1: Conditions for cases & inefficiency

	teams maintained	teams dissolved
decision efficient	$\frac{\lambda}{\delta} \geq \frac{n_{A1}y_1 - n_0(y_1 - y_0)}{n_0 \binom{n_{A1}}{n_{A0}} y_1 - y_0} (*)$	$\frac{\lambda}{\delta} < \frac{n_{A1}y_1 - n_0(y_1 - y_0)}{n_0 \binom{n_{A1}}{n_{A0}} y_1 - y_0}$
decision inefficient	-	$\frac{\lambda}{\delta} > \frac{n_{A0}y_0}{n_0 y_1 - n_{A0}y_0} \ \& (*) \ \& n_0 < n_{A1}$
AI use inefficient	$\frac{\lambda}{\delta} > \frac{(1 - \phi)n_{A0}}{n_0^2 \left(\phi \frac{y_1 - y_0}{y_0} + 1 \right) + (1 - \phi)(n_{A0} + 1)}$	$\frac{\lambda}{\delta} > \frac{1}{n_0} \left[1 - \phi \frac{n_0 \frac{y_1}{y_0} - (n_0 + 1)}{\phi n_{A1} \frac{y_1}{y_0} + (1 - \phi)n_{A0} - 1} \right]$

Notes: The columns 'teams maintained' and 'teams dissolved' contain (in)efficiency requirements when the economy is in the given type of equilibrium. The first row gives the condition under which that is the optimal choice given that AI is available. The middle column gives the condition under which dissolving teams is dynamically inefficient. The bottom row gives the conditions in each equilibrium for AI to lead to dynamic inefficiency.

dynamic inefficiency is the speed of learning, λ/δ . The higher is λ/δ , the more likely it is that AI will lead to a long-run reduction in GDP. A natural question that arises is whether improvements in the capability of AI eventually resolve the dynamic inefficiency.

To answer this question, consider the impact of AI capability improvements on juniors and in seniors. For $z_A \leq z_0$ increases in AI capability increase n_{A0} and n_{A1} proportionately. Improvements in the range $(z_0, z_1]$ keep increasing senior solo productivity, while junior productivity is capped at \bar{n}_{A0} . Improvements of z_A past z_1 do not generate any productivity gains, as verification becomes the bottleneck, and senior productivity is maximized at \bar{n}_{A1} . Since the maximum productivity improvement that AI can provide to juniors and to seniors is capped, in general, it is not true that improvements in AI capability will necessarily resolve dynamic inefficiency.

Figure 4 is helpful in understanding how the equilibrium of the model and dynamic inefficiency depends on the value of z_A and λ/δ . The left panel shows this for a lower value of senior value recognition, v_1 , the right for a higher value. The blue regions on the

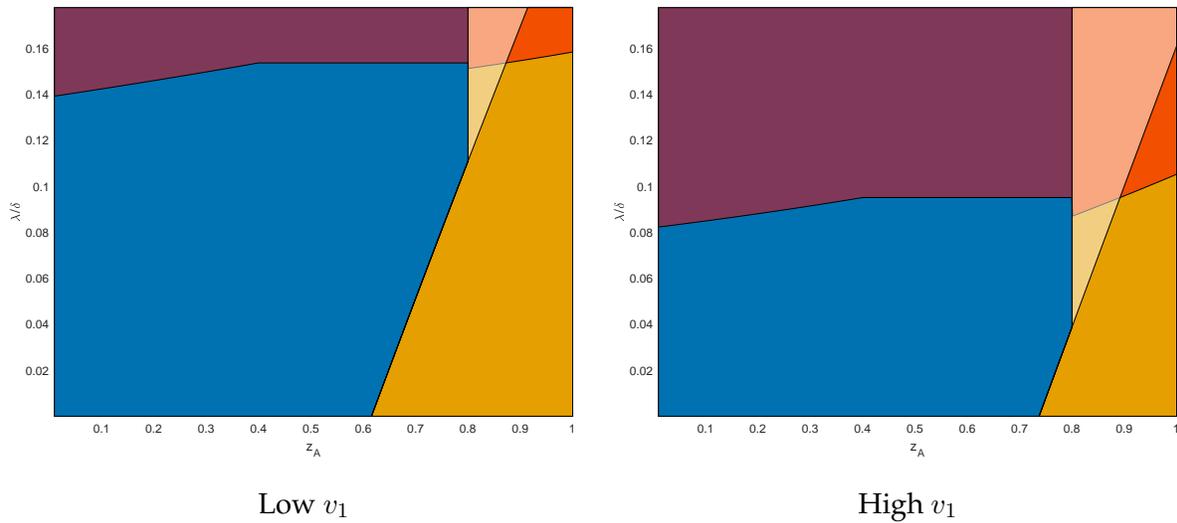


Figure 4: Equilibrium with AI.

Notes: The figure shows the equilibrium with AI for different values of z_A on the horizontal axis, and different values of λ/δ on the vertical axis. The panel on the left is for $v_1 = 3$, on the right if for $v_1 = 8$. In both panels, the blue regions on the left show the region where teams are maintained, the yellow regions the right where teams are dissolved. The top reddish region (composed of 3 different colors) are where AI adoption leads to dynamic inefficiency. The triangular lighter colored region in the middle is where seniors' decision to dissolve teams is dynamically inefficient. The rest of the parameters are: $\phi = 0.05$, $z_0 = 0.4$, $z_1 = 1$, $v_0 = 1$, $h_{A1} = 0.2$, $h_{A2} = h = 0.4$.

left of each panel, where z_A is lower, shows where teams are maintained. If z_A is high enough, then teams are dissolved, this the yellow region on the right of each panel. The upward sloping line that separates the darker yellow region corresponds to the top row

of Table 1, and shows optimal team dissolution. If $\frac{\lambda}{\delta} < \frac{n_{A1}y_1 - n_0(y_1 - y_0)}{n_0 \left(\frac{n_{A1}}{n_{A0}} y_1 - y_0 \right)}$, then there exists a threshold AI capability z_A^* at which it is optimal to dissolve teams. For higher senior value recognition, if λ/δ is high enough, it is possible that there does not exist a z_A for which team dissolution is optimal (in the right panel the straight line crosses the vertical axis on the right). The lighter colored triangular region is where seniors decide to dissolve teams, but this decision creates a dynamic inefficiency in the aggregate economy. This corresponds to the middle row in Table 1. When the speed of learning is high and senior relative to junior AI enhanced productivity is high, learning gains cannot be fully internalized. Seniors' decision to dissolve teams is privately optimal, but it leads to lower long-run GDP than if they maintained teams with juniors using AI. The top reddish regions are where the adoption of AI creates a dynamic inefficiency relative to the economy without AI. This corresponds to the bottom row in Table 1. For any value of z_A there is a high enough learning speed, such that the adoption of AI is dynamically inefficient.⁵ It is notable that the slope of the required z_A is quite small, implying that if AI adoption is dynamically inefficient for low values of z_A , the economy is likely to remain dynamically inefficient despite increases in z_A . This figure shows that AI can be dynamically inefficient whether teams are maintained or not, and whether seniors' decision is dynamically efficient or not.

5 Sources of inefficiency

We have shown that AI can lead to dynamic inefficiency even when individual decisions are efficient. Table 2 summarizes the efficiency of seniors' decision and of AI adoption in the different model specifications.

⁵We only consider λ/δ values where juniors remain abundant even in the steady state of the team equilibrium.

Table 2: Summary of Efficiency Results

Learning regime	Pricing regime	Efficiency of Seniors' decision AI use	
No learning		Yes	Yes
Learning-by-mentoring	non-internalized gains	No	No
Learning-by-mentoring	internalized gains	Yes	No

Notes: The column 'Seniors' decision' refers to whether the decision to maintain or dissolve teams maximizes GDP given AI availability. The column 'AI use' refers to whether AI adoption raises long-run GDP compared to the no-AI steady state.

Our analysis identifies two fundamentally different sources of inefficiency.

The first source is a well-known one, which is incorrectly priced learning. If seniors do not internalize the value of the mentoring they provide, then when they dissolve teams in favor of AI, they ignore the loss of human capital formation. This pecuniary externality can be solved with wage adjustments: if juniors accept lower wages to compensate seniors for training, the externality is internalized, and seniors' decisions become efficient. If junior wages are too low to fully internalize learning gains, then seniors might make dynamically inefficient decisions for the aggregate economy.

The second source is the central finding of the paper, which arises from the *bundling of learning and work*. AI raises junior productivity, increasing their productivity. But the senior's capacity constraint, the maximum number of junior problems they can handle, is unchanged. Therefore, fewer juniors are needed in teams, and fewer juniors learn. This crowding out of learning opportunities *cannot* be solved with wages alone. This is the paper's central finding: the bundling of learning and work creates an irreducible friction that makes AI adoption dynamically inefficient even when all decisions are privately optimal.

Why can't wages alone rule out both of these inefficiencies? The economy has three goods: (1) problem solutions, (2) senior supervision, and (3) learning. But there are only two prices: junior wage and senior wage. If wages fully internalize the gains from learn-

ing, then seniors always make the efficient choice. However, there aren't any prices that can rule out the second type of inefficiency. This inefficiency arises because learning and work are bundled in the apprenticeship model: a junior cannot learn separately, they can only learn from working in a team. But AI unbundles productivity from learning. A senior with AI becomes more productive, which might push them to dissolve teams. A junior with AI produces more output and hence the teams optimally become smaller. AI *reduces* learning opportunities per junior, because some juniors are crowded out from learning. The market cannot separately price these two effects.

We assume that the learning speed, λ is independent from the number of juniors, n , who work with each senior. This assumption reflects the idea that *knowledge is non-rival*, or more precisely that learning is non-rival. Our assumption is stark: learning is as efficient in large teams as it is in small teams. Could it be that when smaller teams are maintained with AI, the learning speed of each apprentice is higher and this undoes the learning loss? This is a possibility, but as long as learning is somewhat non-rival, in so far as training n juniors is not n times less efficient than training one junior, then dynamic inefficiency can arise.⁶ Therefore, as long as learning is non-rival to some extent, learning calls for large teams. But for production purposes, with AI, teams should be small, as each junior handles more problems. These two objectives conflict. Note that when teams are dissolved by seniors, no learning occurs, and AI can be dynamically inefficient, independent of how learning speed depends on team size.

Another possible way to prevent the loss in learning is via *part-time apprenticeships* could help. Seniors could manage the same amount of juniors, if each junior only worked $1/n_A$ time for the senior and $(n_A - 1)/n_A$ time solo with AI. This would maintain learning while capturing AI productivity gains. But this requires that juniors' productivity scales linearly with time, i.e., that jobs are divisible, and requires that learning does not depend on the time spent working with a senior. However, it is likely that there is a minimum time threshold for learning, and part-time jobs usually pay less per hour than full-time

⁶Even if the speed of learning declines with the number of juniors, as long as $n\lambda(n)$ is increasing in n , the possibility for dynamic inefficiency remains.

jobs, suggesting that productivity does not scale linearly with time.

6 Conclusion

We developed a model of AI adoption in knowledge work where seniors and juniors differ in problem-solving skills and value recognition, and juniors learn by working alongside seniors. The model yields three main insights.

First, the bundling of learning with work creates a friction that no market mechanism can fully resolve: AI raises junior productivity but shrinks teams, reducing learning opportunities even when seniors' decisions are privately optimal. Second, AI creates static gains but can cause dynamic losses. When seniors use AI instead of hiring juniors, or when juniors use AI and teams shrink, fewer workers acquire senior skills through mentoring. The long-run supply of seniors falls, and steady-state GDP can decline even as short-run output rises. Third, efficiency depends critically on institutional arrangements. When learning is internalized through wage negotiations, seniors' decisions are efficient. But dynamic inefficiency arises from two distinct sources: seniors not internalizing the value of mentoring (a pecuniary externality that wage adjustments can address), and the bundling friction (which wage adjustments cannot).

Key mechanisms for policy. Several features matter for policy. The value recognition gap, $v_1 > v_0$, persists even as AI's problem-solving capability improves. Seniors' comparative advantage in selecting high-value problems ensures that human mentorship retains value even in a future with high AI capability. The senior capacity constraint—the maximum number of junior problems a senior can handle—is unchanged by AI. This means that AI does not improve team output; it only shrinks teams. The gains from AI come from smaller teams and higher solo productivity, not from enhanced team performance. Finally, learning and work are bundled in the apprenticeship model. A junior learns by being present while working for a senior. AI unbundles productivity from learning: a junior with AI produces more but does not learn faster. Part-time arrangements could

help—each junior works some time for a senior and some time solo with AI—but require divisible jobs and a learning technology that does not depend on the time spent with a senior.

Policy implications. Several policies could mitigate the adverse effects of AI on learning. Tax credits for training expenses or apprenticeship programs would help firms internalize the long-run cost of lost human capital. Subsidies for firms that maintain robust junior training, or industry-specific requirements for minimum mentoring ratios, could preserve learning opportunities. Historically, professions like medicine and law have guild-like systems ensuring knowledge transfer through residencies and clerkships. In an AI era, updated versions of these arrangements could focus on tasks AI cannot do—particularly value recognition and customer relationships.

Limitations and extensions. We treated skill levels, communication costs, and AI capability as exogenous. In reality, these evolve together. AI productivity improves as models learn from data (Wang and Wong (2025)); human skills respond to AI presence through changes in education and training, or AI could assist humans in learning on the job. Incorporating such feedback is an important extension. We also abstracted from heterogeneity in AI adoption across tasks; Koren et al. (2026a) model how AI spreads across different task directions, which could generate richer dynamics.

We assumed learning happens only through mentoring. Alternative pathways exist: Brynjolfsson et al. (2025) show that AI can accelerate learning by codifying expert knowledge and providing real-time feedback. If juniors could acquire skills faster with AI assistance, the dynamic losses we identify would be mitigated. Exploring when AI complements rather than substitutes for mentorship is a promising direction.

Finally, we abstracted from firm heterogeneity and strategic considerations. Firms differ in their reliance on tacit knowledge and mentorship; some may find AI more disruptive than others. Strategic interactions—where one firm’s AI adoption affects the labor market for all—could generate additional externalities. We leave these extensions for fu-

ture work.

References

- ACEMOGLU, D. AND P. RESTREPO (2018): "The Race between Man and Machine: Implications of Technology for Growth, Factor Shares, and Employment," *American Economic Review*, 108, 1488–1542.
- (2020): "Robots and Jobs: Evidence from US Labor Markets," *Journal of Political Economy*, 128, 2188–2244.
- ARROW, K. J. (1962): "The Economic Implications of Learning by Doing," *The Review of Economic Studies*, 29, 155–173.
- BECKER, G. S. (1962): "Investment in Human Capital: A Theoretical Analysis," *Journal of Political Economy*, 70, 9–49.
- BEN-PORATH, Y. (1967): "The Production of Human Capital and the Life Cycle of Earnings," *Journal of Political Economy*, 75, 352–365.
- BERAJA, M. AND F. J. BUERA (2026): "The Life-cycle of Concentrated Industries," Working Paper 34770, National Bureau of Economic Research.
- BRYNJOLFSSON, E., B. CHANDAR, AND R. CHEN (2025): "Canaries in the Coal Mine? Six Facts about the Recent Employment Effects of Artificial Intelligence," Tech. rep., Stanford Digital Economy Lab.
- BURSTEIN, A. T. AND A. MONGE-NARANJO (2009): "Foreign Know-How, Firm Control, and the Income of Developing Countries*," *The Quarterly Journal of Economics*, 124, 149–195.
- CAICEDO, S., J. LUCAS, ROBERT E., AND E. ROSSI-HANSBERG (2019): "Learning, Career Paths, and the Distribution of Wages," *American Economic Journal: Macroeconomics*, 11, 49–88.
- GARICANO, L. (2000): "Hierarchies and the Organization of Knowledge in Production," *Journal of Political Economy*, 108, 874–904.
- GARICANO, L. AND E. ROSSI-HANSBERG (2006): "Organization and Inequality in a Knowledge Economy*," *The Quarterly Journal of Economics*, 121, 1383–1435.
- HERKENHOFF, K., J. LISE, G. MENZIO, AND G. M. PHILLIPS (2024): "Production and Learning in Teams," *Econometrica*, 92, 467–504.
- HESS, P., S. JANSSEN, AND U. LEBER (2023): "The effect of automation technology on workers' training participation," *Economics of Education Review*, 96, 102438.

- IDE, E. AND E. TALAMÀS (2025): “Artificial Intelligence in the Knowledge Economy,” *Journal of Political Economy*, 133, 3762–3800.
- JAROSCH, G., E. OBERFIELD, AND E. ROSSI-HANSBERG (2021): “Learning From Coworkers,” *Econometrica*, 89, 647–676.
- JOVANOVIĆ, B. (2014): “Misallocation and Growth,” *The American Economic Review*, 104, 1149–1171.
- KOREN, M., Z. L. BÁRÁNY, AND U. WOHAČ (2026a): “The Directions of Technical Change,” Preprint arXiv:2602.12958, arXiv.
- KOREN, M., G. BÉKÉS, J. HINZ, AND A. LOHMANN (2026b): “Vibe Coding Kills Open Source,” Preprint arXiv:2601.15494, arXiv.
- LUCAS, R. E. (1988): “On the mechanics of economic development,” *Journal of Monetary Economics*, 22, 3–42.
- MUEHLEMANN, S. (2025): “Artificial intelligence adoption and workplace training,” *Journal of Economic Behavior & Organization*, 238, 107206.
- NOY, S. AND W. ZHANG (2023): “Experimental evidence on the productivity effects of generative artificial intelligence,” *Science*, 381, 187–192.
- WANG, P. AND T.-N. WONG (2025): “Artificial Intelligence and Technological Unemployment,” NBER Working Papers 33867, National Bureau of Economic Research, Inc.